

Evolutionary, symbolic, and hybrid algorithms for planning and web-service composition

Artur Niewiadomski
Siedlce University, Poland

Institute of Computer Science, Polish Academy of Sciences, 02.07.2020

Outline

- 1 Introduction
- 2 Abstract Planning
- 3 Genetic Algorithm
- 4 Hybrid Solution of the Abstract Planning Problem
- 5 Concrete Planning
- 6 Simmulated Annealing
- 7 Generalized Extremal Optimization
- 8 Experimental Results

PlanICS Team

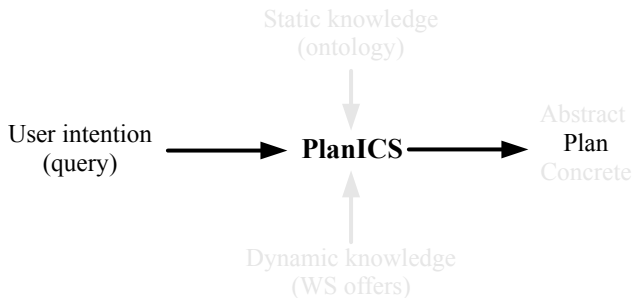
Intelligent hybrid system for planning and composition of web services

- [Wojciech Penczek](#) (ICS PAS, Warsaw)
the Head of the project
- [Artur Niewiadomski](#) (Siedlce University)
symbolic (SMT-based) computations and algorithms
- [Piotr Switalski](#), [Jaroslaw Skaruz](#) (Siedlce University)
Evolutionary (and other nature-inspired) Algorithms
- [Mariusz Jarocki](#), [Agata Polrola](#) (Lodz University)
main concepts and PlanICS language contributors
- [Lukasz Mikulski](#) (Nicolaus Copernicus University, Torun)
Multiset Explorer - plan linearisations
- [Maciej Szreter](#) (ICS PAS, Warsaw)
dynamic Web services

Related work - Web Service Composition Systems

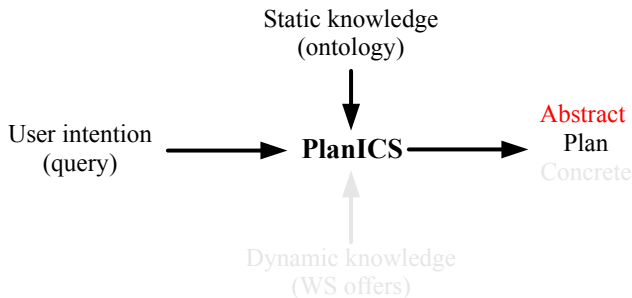
- **Entish** - IOPR, a two phase planning by an ontology,
- **WSMO** - ontology, IOPR, a formal goal, embedded rule languages
- **WSMX** - WSMO implementation, service registration, service discovery by matchmaking, service activation by adapters
- **SUPER** - composition based on WSMO ontology and AI algorithms
- **PlanICS**
 - a state-based approach, multi-phase planning, a simple rule language,
 - abstract planners based on **GA**, **SMT**-solvers, and combining both as **hybrid planners**,
 - concrete planners based on evolutionary algorithms, **SMT**-solvers, and hybrid ones.

Key Concepts



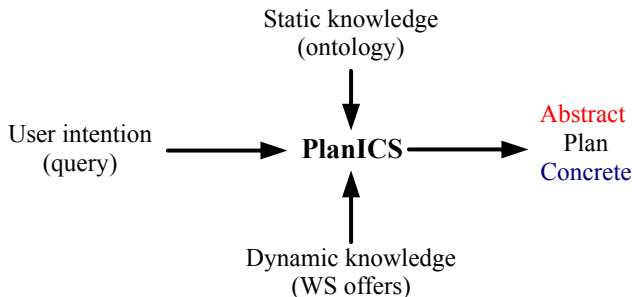
- The main goal: an **arrangement of service executions** satisfying a user intention

Key Concepts



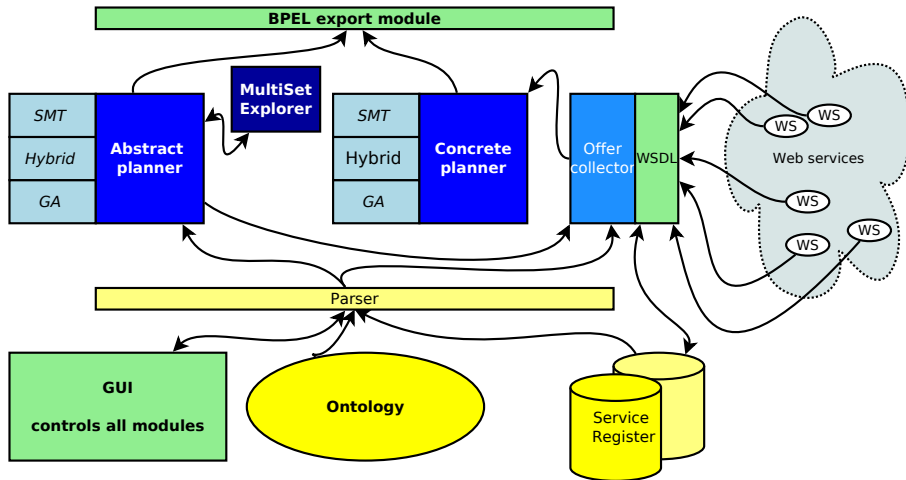
- The main goal: an **arrangement of service executions** satisfying a user intention
- Ontology - the **types** of services and objects

Key Concepts

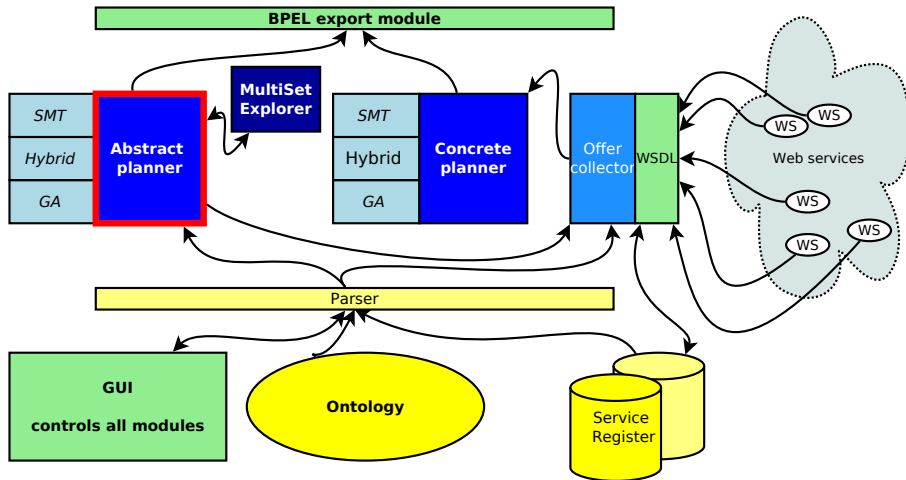


- The main goal: an **arrangement of service executions** satisfying a user intention
- Ontology - the **types** of services and objects
- A **two phase composition** process: **abstract** (on types) and **concrete** (on web services)

System Overview



System Overview



Abstract Planning Phase

Planning in the terms of

- Service types
- Object types
- Abstract values of object attributes

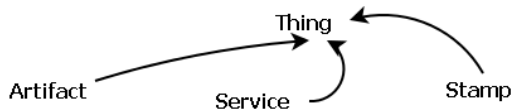
Basic concepts

- A **world** - a set of objects with specific attribute values
- A **service** can **transform** a world (if the pre-condition is met) by changing attribute values of existing objects and adding new objects
- A user **query** specifies **initial** and **expected** (final) worlds
- A **solution** is a **sequence** of **service types** able to transform an initial world into a world matching an expected one
- A **plan** is a set of solutions built over the same **multiset** of service types, regardless the ordering and the contexts.

Main goals of abstract planning

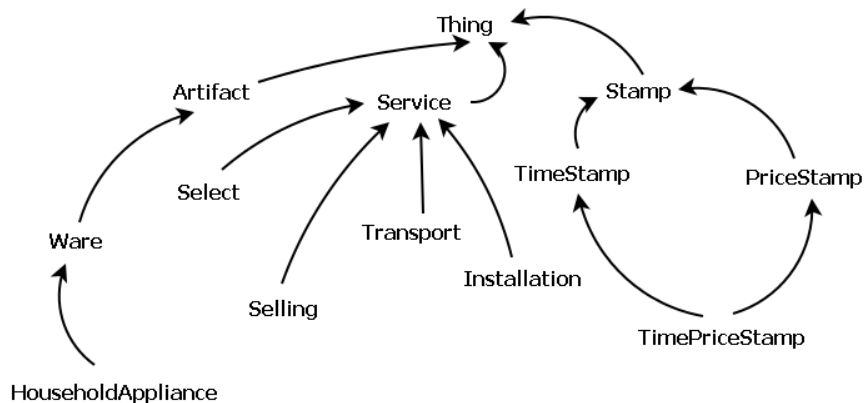
- Checking whether the user query can be realized using a given ontology
- Reducing the search space for a concrete planner
- Reducing the number of network interactions between web services and offer collector
- Providing a number of different potential ways to realize the query

Ontology



- OWL + embedded PlanICS language
- Service types
- Artifacts - objects the services operate on
- Stamps - special objects describing certain execution features

Ontology Example



User Query and Abstract Plan Example

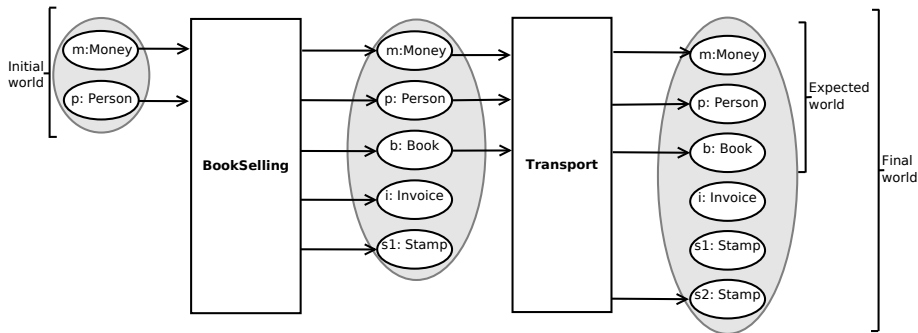
in $\{p : \text{Person}\}$

inout $\{m : \text{Money}\}$

out $\{b : \text{Book}\}$

pre ($p.\text{name} = \text{ME}$ and $p.\text{address} = \text{MyAddr.}$ and $m.\text{amount} = 50$)

post ($b.\text{title} = \text{"Java in Practice"}$ and $b.\text{location} = p.\text{address}$)



SMT-based abstract planning

$$\varphi_k^q = \mathcal{I}^q \bigwedge_{i=1..k} \left(\mathcal{C}_i \bigvee_{s \in \mathbb{S}} \mathcal{T}_i^s \right) \wedge \mathcal{E}_k^q \wedge \mathcal{B}_k^q$$

- Abstract planning problem for a query q encoded as the formula φ_k^q
- φ_k^q satisfiable iff there exists a solution for q of the length k
- If a solution is found, then block all known abstract plans with the formula \mathcal{B}_k^q and search for other solutions,
- Otherwise proceed with $k + 1$

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The formula φ_k^q encodes

- **the initial worlds**
- contexts and worlds transformations
- the expected worlds
- a blocking formula

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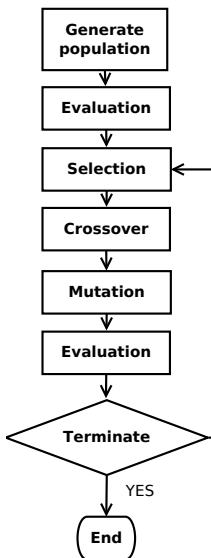
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Genetic Algorithm



- Introduced in 1960 by John Holland
- Applied to optimization and search problems
- A population of individuals (candidate solutions) is evolved toward better solutions
- Operators: mutation, crossover and selection
- Problem specific:
 - Encoding of individuals
 - Fitness function
 - Versions of operators and probabilities of their application

An individual is represented usually by a fixed-length array of bits or numbers. The fitness function evaluates a candidate solution - we know which ones are better than others. The better individuals have more chances to move on to the next stages of the algorithm.

GA-based abstract planning

- Standard GA implementation, but sophisticated fitness function and specialised mutation operator
- Individual: a sequence of service types
- Genes reordering in order to find the longest executable prefix
- **Good service type** concept

Intuitively, a service type is good, if it produces objects that can be a part of the expected world, or they can be an input for other good service types.

Individual of GA

An individual

- a multiset M of service types.

Abstract plan

Selling \rightarrow Payment \rightarrow Transport

Individual of GA

1	6	3
---	---	---

Set of all services and their indexes

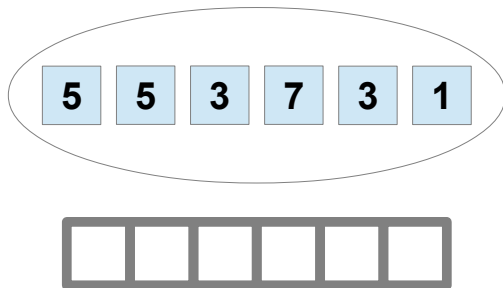
Index	Service
1	Selling
...	...
3	Transport
...	...
...	...
6	Payment



Sequence from Multiset

Checking whether M is a plan

A transformation sequence seq_M is constructed from M .

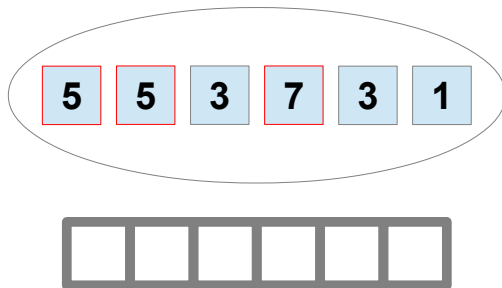


- Start from an empty sequence

Sequence from Multiset

Checking whether M is a plan

A transformation sequence seq_M is constructed from M .

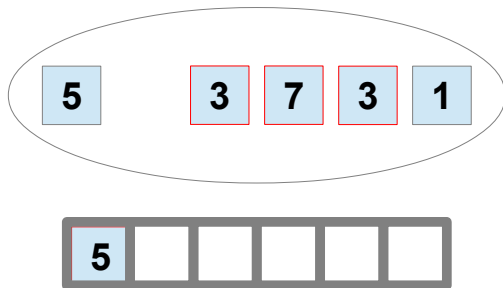


- Service types able to transform an initial world

Sequence from Multiset

Checking whether M is a plan

A transformation sequence seq_M is constructed from M .

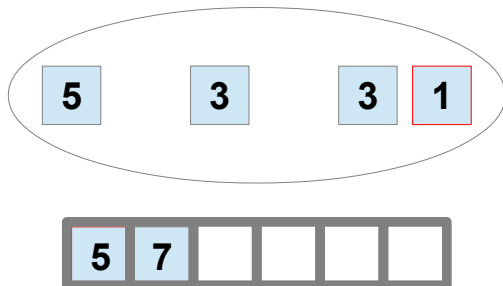


- Choose one, append it to seq_M ...

Sequence from Multiset

Checking whether M is a plan

A transformation sequence seq_M is constructed from M .

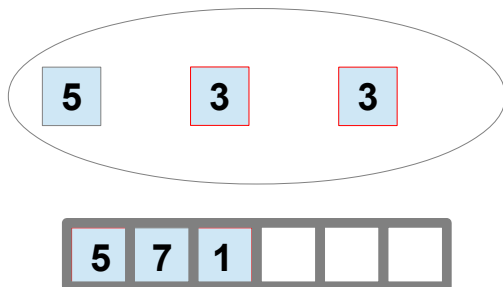


- ...and check which Service Type can transform the current world

Sequence from Multiset

Checking whether M is a plan

A transformation sequence seq_M is constructed from M .

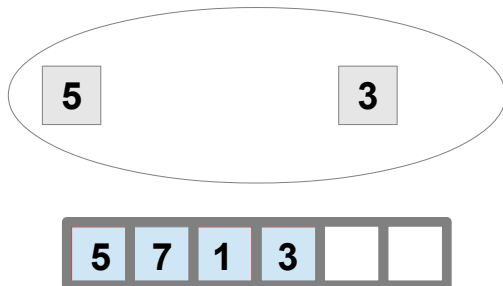


- ...append and check next ...

Sequence from Multiset

Checking whether M is a plan

A transformation sequence seq_M is constructed from M .

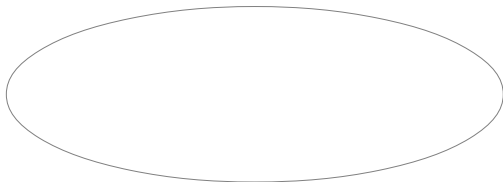


- If none of remaining Service Types can transform the current world

Sequence from Multiset

Checking whether M is a plan

A transformation sequence seq_M is constructed from M .



- Append all to seq_M

Fitness function

$$fitness_M = \frac{f_{wM} * \alpha + c_{wM} * \beta + l_M * \gamma + g_{seqM} * \delta}{|w_q| * \alpha + |w_q| * \beta + |M| * \gamma + |M| * \delta} \quad (1)$$

- f_{wM} is the maximal number of objects from w_M , which **types and valuations** are consistent with objects from an expected world,
- $c_{wM} = \min(\text{cst}(w_M), |w_q|)$, where $\text{cst}(w_M)$ is the number of the objects from w_M of **types** consistent with an expected world
- g_{seqM} is the number of the good service types occurring in seq_M ,
- l_M is the length of the executable prefix of seq_M
- $\alpha = 0.1$, $\beta = 0.7$, $\gamma = 0.1$, and $\delta = 0.2$ are parameters of the fitness function.

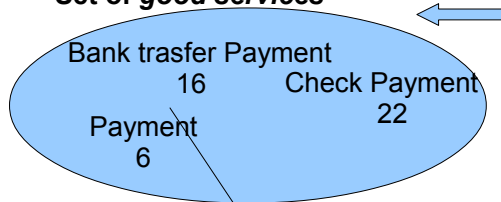
After finding the first solution, the fitness function is modified by a penalty for similarity of new solutions to those already found.

Mutation operator

Individual of GA before mutation

1	7	3
---	---	---

Set of *good services*



1	6	3
---	---	---

Individual of GA after mutation

Set of all services and their indexes

Index	Service
1	Selling
...	...
3	Transport
...	...
6	Payment
7	Paint a bike
...	...

Hybrid Solution

Motivation

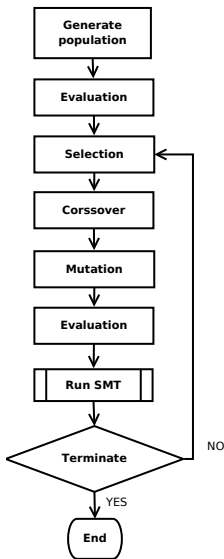
- Advantages and disadvantages of both methods: **SMT** and **GA**

	SMT	GA
Short time	X	✓
High probability	✓	X

Solution

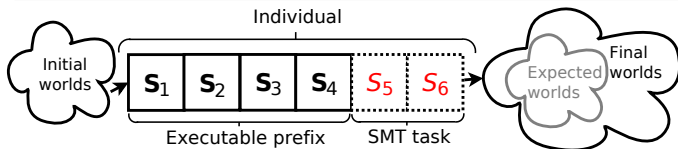
- Combine both algorithms to exploit their advantages

Main Concept of Hybrid Abstract Planner



SMT-based procedure

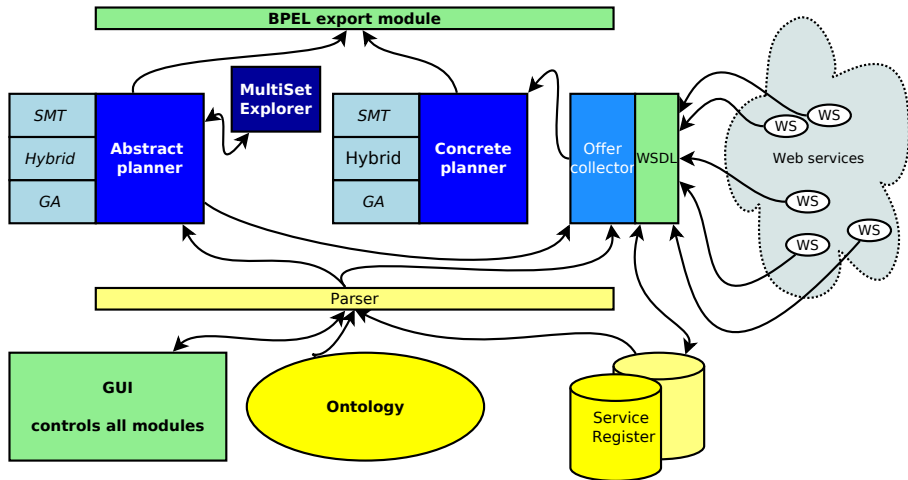
- searching for a new suffix of an individual
- the individuals passed to SMT have to
 - consist at least in a half of good service types, and
 - at least a half of their genes should constitute an executable prefix.



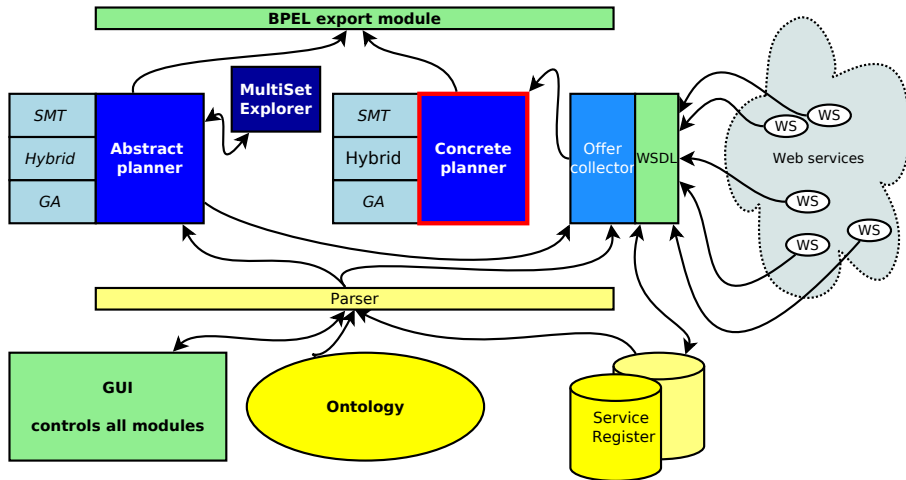
Experimental results

Exp	k	n	sol	Hybrid						Pure GA				Pure SMT	
				SMT [s]	GA [s]	Total [s]	Avg plans	Max plans	Prob. [%]	Time [s]	Avg plans	Max plans	Prob. [%]	First [s]	Total [s]
1	6	64	1	4.05	8.24	12.29	1	1	100	5.71	1	1	100	6.31	12.8
2		128		5.77	8.78	14.55	1	1	100	8.07	1	1	100	7.29	14.8
3		256		10.79	13.29	24.07	1	1	100	13.62	1	1	100	16.66	27.1
4		64	10	3.04	25.74	28.78	3.25	10	100	24.29	5.4	10	100	5.22	18.3
5		128		6.52	32.15	38.67	3.15	8	100	31.21	6.25	10	100	8.54	26.6
6		256		13.85	43.33	57.18	3.65	8	100	45.95	5.55	9	100	11.93	38.1
7	9	64	1	12.08	11.67	23.75	1	1	85	11.83	1	1	95	19.49	58.7
8		128		25.65	15.68	41.33	1	1	90	13.43	1	1	100	41.01	90.1
9		256		43.61	28.88	72.49	1	1	90	26.74	1	1	90	54.99	133
10		64	10	17.54	56.9	74.43	3.15	10	100	57.69	1.77	4	65	21.09	295
11		128		30.64	63.38	94.02	4.16	10	95	69.94	1.54	4	65	49.93	553
12		256		61.64	113.05	174.69	4.32	10	95	113.15	1.33	2	30	113.3	977
13	12	64	1	55.09	21.77	76.86	1	1	45	21.22	1	1	65	156.4	781
14		128		86.48	30.15	116.62	1	1	85	28.12	1	1	60	203.2	1962
15		256		118.7	46.82	165.52	1	1	55	46.31	1	1	60	315.4	1947
16		64	10	78.98	118.56	197.54	2.79	10	95	118.29	0	0	0	113.5	> 2000
17		128		109.89	139.96	249.84	2.38	10	80	148.65				250.5	
18		256		193.17	253.22	446.39	1.85	6	65	260.94				325.8	
19	15	64	1	119.09	33.68	152.77	1	1	25	34.56	1	1	30	469.7	
20		128		185.34	43.17	228.51	1	1	30	40.45	1	1	25	382.1	
21		256		247.3	68.26	315.56	1	1	35	68.69	1	1	35	1018	
22		64	10	168.46	237.57	406.03	1.67	3	30	216.6	0	0	0	413	
23		128		309.53	267.83	577.36	3	5	10	261.21				1850	
24		256		304.88	450.63	755.5	3	3	5	437.59				931	

System Overview

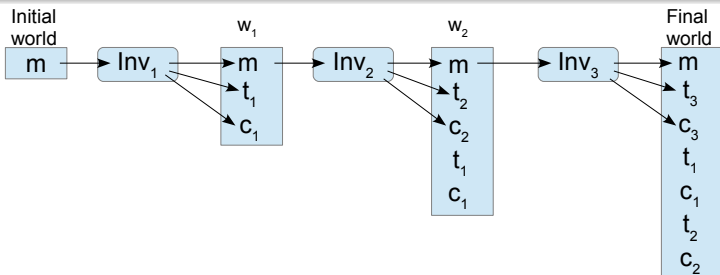


System Overview



Abstract Plan, Offers, Constraints

Query: 3 investments up to \$100, maximizing the sum of profits



$$\begin{bmatrix} o_{1,1}^1 & \dots & o_{1,5}^1 \\ \vdots & \ddots & \vdots \\ o_{k_1,1}^1 & \dots & o_{k_1,5}^1 \end{bmatrix} \begin{bmatrix} o_{1,1}^2 & \dots & o_{1,5}^2 \\ \vdots & \ddots & \vdots \\ o_{k_2,1}^2 & \dots & o_{k_2,5}^2 \end{bmatrix} \begin{bmatrix} o_{1,1}^3 & \dots & o_{1,5}^3 \\ \vdots & \ddots & \vdots \\ o_{k_3,1}^3 & \dots & o_{k_3,5}^3 \end{bmatrix}$$

Attributes: $m.amount$ $t_i.amount$ $t_i.profit$ $c_i.fee$ $m.amount'$

Variables: $o_{j,1}^i$ $o_{j,2}^i$ $o_{j,3}^i$ $o_{j,4}^i$ $o_{j,5}^i$

Constraint: $\sum_{i=1}^3 o_{j,2}^i \leq 100,$ **Quality function:** $\sum_{i=1}^3 o_{j,3}^i$

Concrete Planning as the Constrained Optimization Problem

$$P_j^i = [o_{j,1}^i, o_{j,2}^i, \dots, o_{j,m_i}^i]$$

\mathbb{P} : the set of all possible sequences $(P_{j_1}^1, \dots, P_{j_n}^n)$,

$$\max\{Q(S) \mid S \in \mathbb{P}\} \text{ subject to } \mathbb{C}(S),$$

- $Q : \mathbb{P} \mapsto \mathbb{R}$,
an objective function defined as the sum of all quality constraints
- $\mathbb{C}(S)$, where $S \in \mathbb{P}$,
a set of constraints to be satisfied.

A solution of CPP

- selecting one offer from each offer set
 - all constraints are satisfied
 - value of the objective function is maximized

SMT-based algorithm overview

SMT(Satisfiability Modulo Theories)

- Encode CPP as a formula $[\varphi]$ which is satisfiable iff there is a solution
- Exploit an SMT-solver to find a solution of quality q , where $q \in \mathbb{R}$
- Proceed with $[\varphi] \wedge [quality > q]$ to search for better solutions
 - adapting the binary search method
 - taking advantage of SMT interactive mode
 - using assumptions

GA for Concrete Planning Problem

Standard GA implementation

- Individual - a sequence of indices of the offers chosen from the consecutive offer sets,
- $fitness(Ind) = Q(S_{Ind}) + \beta \cdot \frac{|sat(\mathbb{C}(S_{Ind}))|}{c}$,
 - Ind - an individual,
 - S_{Ind} - a sequence of the offer values corresponding to Ind ,
 - $sat(\mathbb{C}(S_{Ind}))$ - a set of the constraints satisfied by Ind ,
 - c - the number of all constraints,
 - β - a constant to reduce both of the sum components to the same order of magnitude.

Simulated Annealing (SA)

- a probabilistic metaheuristic
- the annealing process in metallurgy - heating and cooling of a material in order to improve its properties
- in SA “a material” is a potential solution - **an individual**
- cooling implemented as a slow decrease in the probability of accepting worse solutions while the algorithm explores the search space
- search space exploration by applying a neighbourhood operator to the individual in order to obtain a new individual
 - usually, a neighbourhood operator is like mutation in GA, but applied with the probability equals to 1
 - in our case it changes one randomly chosen “gene- an offer index

SA Algorithm for Concrete Planning

SA($n, G, I_L, temp, decFactor$)

Input: the length of the individual: n , the number of iterations: G , the number of internal loop iterations: I_L , an initial value of the temperature: $temp$, the temperature decreasing factor: $decFactor$

Result: a solution of the highest quality function value

begin

```
 $I_{cur} \leftarrow random(n)$  ; // generate an individual randomly
 $Q_{cur} \leftarrow Q(I_{cur})$  ; // calculate the quality of the initial individual
 $Q_{best} \leftarrow Q_{cur}$  ; // remember the best quality found so far
 $I_{best} \leftarrow I_{cur}$  ; // store the best solution found so far
for ( $i \leftarrow 1..G$ ) do
    for ( $j \leftarrow 1..I_L$ ) do
         $I_{new} \leftarrow neighbourhood(I_{cur})$  ; // generate a new individual
        if ( $I_{new}$  satisfies all constraints) then
             $Q_{new} \leftarrow Q(I_{new})$  ; // calculate the quality of the new individual
            if ( $(Q_{new} > Q_{cur}) \vee (random([0.0, 1.0]) < exp(\frac{Q_{new} - Q_{cur}}{temp}))$ ) then
                 $I_{cur} \leftarrow I_{new}$  ;
                 $Q_{cur} \leftarrow Q_{new}$  ;
                if ( $Q_{cur} > Q_{best}$ ) then
                     $Q_{best} \leftarrow Q_{cur}$  ; // update the best quality value found
                     $I_{best} \leftarrow I_{cur}$  ; // update the best solution - elite
             $temp \leftarrow temp * decFactor$  ; // decrease the temperature
return  $I_{best}$  ;
```

Generalized Extremal Optimization (GEO)

Different terminology!

- Introduced by Sousa et al. about 2004
- The main idea is to focus on the worst parts of a solution and change them
- Similarly to SA maintains a single solution
- At every step, the algorithm
 - tries to mutate **every** gene separately
 - assigns a number proportional to the gain (or loss) of fitness after the change
 - builds a ranking of genes - the most promising have a better chance to mutate
 - stochastically choose and modify a gene from ranking

GEO Algorithm for Concrete Planning

GEO(n, K, τ)

Input: the number of individuals in population: n , the number of iterations: K , a parameter: τ

Result: a solution with the highest fitness value

begin

```
 $I_{cur} \leftarrow \text{random}(n)$  ; // generate an initial offer vector randomly
 $Q_{best} \leftarrow Q(I_{cur})$  ; // calculate and store the best fitness value found so far
 $I_{best} \leftarrow I_{cur}$  ; // remember the best solution found so far
for ( $i \leftarrow 1..K$ ) do
    for ( $j \leftarrow 1..n$ ) do
         $I_{tmp,j} \leftarrow \text{mutation}(I_{cur}, j)$  ; // mutate the  $j$ -th offer index
        if ( $I_{tmp,j}$  satisfies all constraints) then
             $Q_j \leftarrow Q(I_{tmp,j})$  ; // calculate the fitness value of  $I_{tmp,j}$ 
        else
             $Q_j \leftarrow \infty$  ; // individuals violating constraints fall low in the ranking
             $\Delta_j \leftarrow Q_j - Q(I_{cur})$  ; // relative change of fitness resulting from mutation
         $\text{Rank} \leftarrow \text{sort}((I_{tmp,1}, \Delta_1), \dots, (I_{tmp,n}, \Delta_n)), \text{desc}$  ; // build the ranking by sorting the
        mutated populations according to decreasing  $\Delta_j$  values
         $\text{changed} \leftarrow \text{false}$  ;
        while ( $\neg \text{changed}$ ) do
             $j \leftarrow \text{random}(1..n)$  ; // randomly choose an individual to be changed
             $k \leftarrow \text{Rank.find}(j)$  ; // the position of the  $j$ -th individual in the ranking
             $p \leftarrow k^{-\tau}$  ; // the probability of mutation of the  $j$ -th individual
             $x \leftarrow \text{random}([0.0, 1.0])$  ; // a random value from the range [0.0, 1.0]
            if ( $p > x$ ) then
                 $I_{cur} \leftarrow I_{tmp,j}$  ; // a new population becomes the current one
                 $\text{changed} \leftarrow \text{true}$  ;
                if ( $(\infty > Q_j > Q_{best})$ ) then
                     $Q_{best} \leftarrow Q_j$  ; // update the best fitness value found so far
                     $I_{best} \leftarrow I_{cur}$  ; // update the best solution found so far
    return  $I_{best}$  ; // return the best solution
```

Hybrid Solution

Motivation

- Disadvantages of both methods: **SMT** and **Metaheuristics**

	SMT	Metaheuristics
Short time	X	✓
Good quality	✓	X
High probability	✓	X

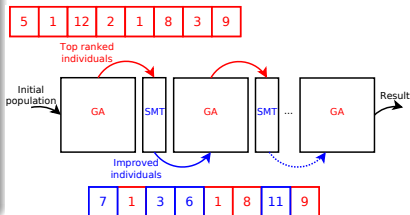
Solution

- Combine both algorithms to exploit their advantages

Hybrid Concrete Planners

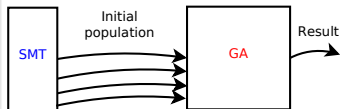
Random Hybrid (RH) and Semi-Random Hybrid (SRH)

- combine **GA** with **SMT**
- alternately run **GA** and **SMT**
- best individuals of **GA** passed to **SMT** for improving



Initial Population Hybrid (IPH)

- **SMT** generates (a part of) the initial population
- the generated individuals satisfy all constraints
- **GA** obtains some (usually not optimal) solutions at start



Hybrid SA and Hybrid GEO

HSA and HGEO

- follows the IPH scheme
- GA replaced by SA or GEO
- the initial solution generated by an SMT procedure
- it satisfies all constraints, but usually is of poor quality

Experiments

- 12 datasets generated randomly, scaled by the length of a plan (10, 15, or 20) and the number of offers ($2^8 = 256$ or $2^9 = 512$)
- the search space varying from $256^{10} = 2^{80}$ to $512^{20} = 2^{180}$

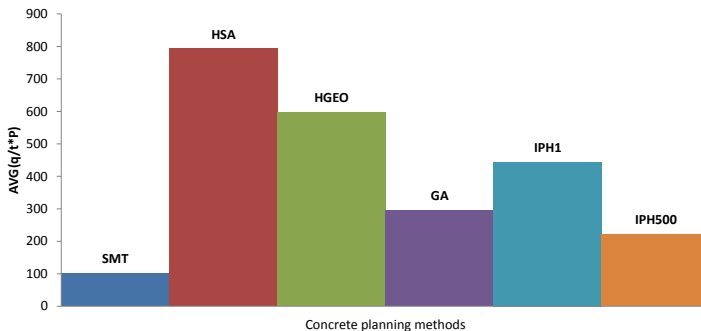
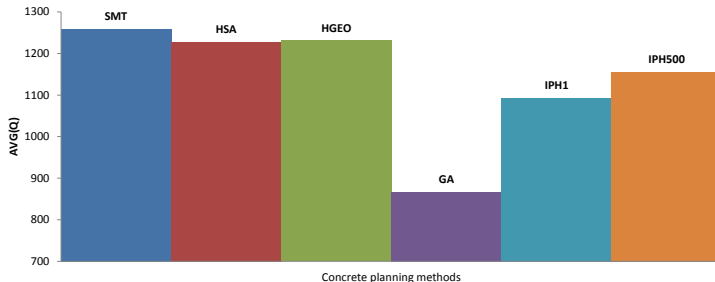
$$\mathbb{C}(S)_{1..6} = \bigwedge_{i=1}^{n-1} (o_{j_i,1}^i < o_{j_{i+1},1}^i), \quad Q_{1..6} = \sum_{i=1}^n o_{j_i,2}^i$$

$$\mathbb{C}(S)_{7..12} = \bigwedge_{i=1}^{n-1} (o_{j_i,1}^i - o_{j_i,2}^{i+1}) > 10, \quad Q_{7..12} = \sum_{i=1}^{n-1} (o_{j_i,1}^i - o_{j_i,2}^{i+1}),$$

Parameters

- IPH and GA: the population size = 1000, iterations = 100, crossover probability 95%, mutation probability 0,5%,
- HSA: $temp = 1.0$, $G = 500$, $I_L = 40$, $decFactor = 0.98$,
- HGEO: $n = 10; 15; 20$, $K = 1000$, $\tau = 5.0$,
- SMT: 400 sec. timeout.

Experimental Results Summary



Conclusions and Future Work

Hybrids are

- methods of a high potential
- a trade-off between time and probability

Future work

- Improve the results of APP and CPP
- Try to combine SMT with other Evolutionary Algorithms
- Develop hybrids for other problems, like, e.g., model checking
- Reductions and abstractions to speed up the planning

Thank You

References

- Combining ontology reductions with new approaches to automated abstract planning of PlanICS. Applied Soft Computing 53 (2017): 352-379, <http://dx.doi.org/10.1016/j.asoc.2017.01.007>
- Concrete Planning in PlanICS Framework by Combining SMT with GEO and Simulated Annealing. Fundam. Inform. 147 (2016): 289-313, IOS Press, 2016. DOI 10.3233/FI-2016-1409
- Hybrid Approach to Abstract Planning of Web Services. Service Computation 2015 : 35-40
- Genetic Algorithm to the Power of SMT: a Hybrid Approach to Web Service Composition Problem. Service Computation 2014: 44-48
- Towards SMT-based Abstract Planning in PlanICS Ontology, in KEOD, pages 123-131, 2013
- Automated abstract planning with use of genetic algorithms, GECCO (Companion) 2013: 129-130
- Evolutionary Algorithms for Abstract Planning, in PPAM (1), vol. 8384 of LNCS, pages 392-401, Springer, 2013
- SMT vs Genetic Algorithms: Concrete Planning in PlanICS Framework, CS&P2013: 309-321, ceur-ws.org/Vol-1032/paper-27.pdf